

1a $y_1 = x^2 \cdot x^3$ en $y_2 = x^5$
komen op hetzelfde neer.

X	y_1	y_2
-2	-32	-32
-1	-1	-1
0	0	0
1	1	1
2	32	32
3	243	243
4	1024	1024

1b $y_1 = \frac{x^6}{x^3}$ en $y_2 = x^2$
komen niet op hetzelfde neer.

X	y_1	y_2
-2	64	4
-1	1	1
0	0	0
1	1	1
2	64	4
3	729	9
4	4096	16

1c $y_1 = (2x^3)^2$ en $y_2 = 4x^6$
komen op hetzelfde neer.

X	y_1	y_2
-2	256	256
-1	4	4
0	0	0
1	4	4
2	256	256
3	2916	2916
4	16384	16384

2a $2a^2 \cdot 4a^3 = 8a^5$.

2d $(-4a)^4 = (-4)^4 \cdot a^4 = 256a^4$.

2g $(-a^3)^3 = -a^9$. $\boxed{5^3} \quad 125$

2b $-5a^7 \cdot a^3 = -5a^{10}$.

2e $-(3a^4)^2 = -3^2 \cdot (a^4)^2 = -9a^8$.

2h $(5a)^3 \cdot -3a = 125a^3 \cdot -3a^1 = -375a^4$.

2c $\frac{-28a^6}{7a} = \frac{-28a^6}{7a^1} = -4a^5$.

2f $(-2a^2)^5 = (-2)^5 \cdot (a^2)^5 = -32a^{10}$.

2i $\left(\frac{9a^4}{a}\right)^2 = (9a^3)^2 = 9^2 \cdot (a^3)^2 = 81a^6$.

3a $(ab)^4 \cdot a = a^4b^4 \cdot a^1 = a^5b^4$.

3d $(3a)^3 - 8a^3 = 27a^3 - 8a^3 = 19a^3$.

3b $(-2ab)^3 \cdot b = -8a^3b^3 \cdot b^1 = -8a^3b^4$.

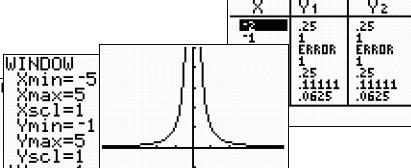
3e $\left(\frac{1}{2}a\right)^2 + (-a)^2 = \frac{1}{4}a^2 + a^2 = 1\frac{1}{4}a^2$.

3c $(3a)^2 + (2b)^2 = 9a^2 + 4b^2$.

3f $(5a^4)^2 + (-a^2)^4 = 25a^8 + a^8 = 26a^8$.

4a De grafieken

van $y_1 = \frac{1}{x^2}$
en $y_2 = x^{-2}$
vallen samen.



5a Exponenten nemen (trap af) steeds met 1 af.

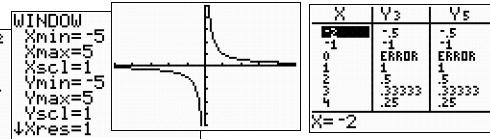
Getallen (achter =) worden steeds door 2 gedeeld.

$$\begin{aligned} 2^5 &= 32 \\ 2^4 &= 16 \\ 2^3 &= 8 \\ 2^2 &= 4 \\ 2^1 &= 2 \\ 2^0 &= 1 \\ 2^{-1} &= \frac{1}{2} \\ 2^{-2} &= \frac{1}{4} \end{aligned}$$

5c $2^{-3} = \frac{1}{8}$ en $2^{-4} = \frac{1}{16}$.

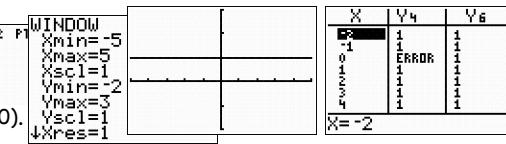
4b De grafieken

van $y_3 = x^{-1}$
en $y_5 = \frac{1}{x}$
vallen samen.



4c De grafieken

van $y_4 = x^0$
en $y_6 = 1$
vallen samen (voor $x \neq 0$).



6a $a^{-5} \cdot a^2 = a^{-5+2} = a^{-3}$.

6d $(a^{-3})^4 = a^{-12}$.

6g $\left(\frac{1}{a^2}\right)^3 = (a^{-2})^3 = a^{-6}$.

6b $a^4 \cdot \frac{1}{a^6} = \frac{a^4}{a^6} = a^{4-6} = a^{-2}$.

6e $a^4 : \frac{1}{a^3} = a^4 : a^{-3} = a^{4-(-3)} = a^7$.

6h $1 = a^0$.

6c $\frac{a^3}{a^2} = a^{3-2} = a^5$.

6f $a^7 : a^0 = a^{7-0} = a^7$.

6i $a^3 \cdot (a^4)^{-2} = a^3 \cdot a^{-8} = a^{3+(-8)} = a^{-5}$.

7a $4^{-3} = \frac{1}{4^3} = \frac{1}{64}$. $\boxed{4^{-3} \rightarrow \text{Frac}} \quad \frac{1}{64}$

7d $\left(\frac{2}{5}\right)^{-2} = \frac{1}{\left(\frac{2}{5}\right)^2} = \frac{1}{\frac{4}{25}} = \frac{25}{4}$. $\boxed{\left(2/5\right)^{-2} \rightarrow \text{Frac}} \quad \frac{25}{4}$

7b $\left(\frac{5}{6}\right)^{-2} = \frac{1}{\left(\frac{5}{6}\right)^2} = \frac{1}{\frac{25}{36}} = \frac{36}{25}$. $\boxed{\left(5/6\right)^{-2} \rightarrow \text{Frac}} \quad \frac{36}{25}$

7e $\left(2\frac{1}{2}\right)^{-2} = \left(\frac{5}{2}\right)^{-2} = \frac{1}{\left(\frac{5}{2}\right)^2} = \frac{1}{\frac{25}{4}} = \frac{4}{25}$. $\boxed{\left(2.5\right)^{-2} \rightarrow \text{Frac}} \quad \frac{4}{25}$

7c $\left(3^{-1}\right)^4 = 3^{-4} = \frac{1}{3^4} = \frac{1}{81}$. $\boxed{\left(3^{-1}\right)^4 \rightarrow \text{Frac}} \quad \frac{1}{81}$

7f $1 : \left(\frac{3}{7}\right)^{-2} = \frac{1}{\left(\frac{3}{7}\right)^{-2}} = \left(\frac{3}{7}\right)^2 = \frac{9}{49}$. $\boxed{1/\left(3/7\right)^{-2} \rightarrow \text{Frac}} \quad \frac{9}{49}$

8a $6a^{-3} \cdot b^2 = 6 \cdot \frac{1}{a^3} \cdot b^2 = \frac{6b^2}{a^3}$.

8c $2a^{-3} = 2 \cdot \frac{1}{a^3} = \frac{2}{a^3}$.

8e $3a^{-2} \cdot b^3 = 3 \cdot \frac{1}{a^2} \cdot b^3 = \frac{3b^3}{a^2}$.

8b $\frac{1}{3}a^{-4} = \frac{1}{3} \cdot \frac{1}{a^4} = \frac{1}{3a^4}$.

8d $3a \cdot b^{-2} = 3a \cdot \frac{1}{b^2} = \frac{3a}{b^2}$.

8f $(3a)^{-2} \cdot 2b^{-1} = \frac{1}{(3a)^2} \cdot 2 \cdot \frac{1}{b} = \frac{1}{9a^2} \cdot \frac{2}{b} = \frac{2}{9a^2b}$.

9a De functies $f(x) = \sqrt{x}$ en $g(x) = x^{\frac{1}{2}}$ komen op hetzelfde neer.

X	y_1	y_2
-1	ERROR	ERROR
0	0	0
1	1	1
2	1.4142	1.4142
3	1.7321	1.7321
4	2	2

9b De grafieken van $h(x) = \sqrt[3]{x}$ en $k(x) = x^{\frac{1}{3}}$ vallen samen.

X	y_1	y_2
-2	-1.26	-1.26
-1	-1	-1
0	0	0
1	1	1
2	1.26	1.26
3	1.4822	1.4822
4	1.5874	1.5874

10a \blacksquare	$5^{\frac{1}{3}} = \sqrt[3]{5}$.	10c \blacksquare	$2a^{\frac{2}{5}} = 2 \cdot \sqrt[5]{a^2}$.	10e \blacksquare	$4a^{-2}b^{\frac{1}{2}} = 4 \cdot \frac{1}{a^2} \cdot \sqrt{b} = \frac{4 \cdot \sqrt{b}}{a^2}$.
10b \blacksquare	$7^{-\frac{1}{3}} = \frac{1}{7^{\frac{1}{3}}} = \frac{1}{\sqrt[3]{7}}$.	10d \blacksquare	$-a^{-\frac{3}{5}} = -\frac{1}{a^{\frac{3}{5}}} = -\frac{1}{\sqrt[5]{a^3}}$.	10f \blacksquare	$3a^{\frac{1}{3}}b^{-\frac{1}{2}} = 3 \cdot \sqrt[3]{a} \cdot \frac{1}{b^{\frac{1}{2}}} = \frac{3 \cdot \sqrt[3]{a}}{\sqrt{b}}$.
11a \blacksquare	$\sqrt{x} = x^{\frac{1}{2}}$.	11e \blacksquare	$\frac{\sqrt{x}}{\sqrt[3]{x}} = \frac{x^{\frac{1}{2}}}{x^{\frac{1}{3}}} = x^{\frac{1}{2}-\frac{1}{3}} = x^{\frac{3}{6}-\frac{2}{6}} = x^{\frac{1}{6}}$.		
11b \blacksquare	$x \cdot \sqrt[4]{x} = x^1 \cdot x^{\frac{1}{4}} = x^{\frac{5}{4}}$.	11f \blacksquare	$\sqrt{x} \cdot \sqrt[3]{x^2} = x^{\frac{1}{2}} \cdot x^{\frac{2}{3}} = x^{\frac{1}{2}+\frac{2}{3}} = x^{\frac{3}{6}+\frac{4}{6}} = x^{\frac{7}{6}}$.		
11c \blacksquare	$\frac{1}{\sqrt[3]{x^2}} = \frac{1}{x^{\frac{2}{3}}} = x^{-\frac{2}{3}}$.	11g \blacksquare	$\frac{x^2}{\sqrt[4]{x^3}} = \frac{x^2}{x^{\frac{3}{4}}} = x^{2-\frac{3}{4}} = x^{\frac{5}{4}}$.		
11d \blacksquare	$\sqrt[5]{\frac{1}{x}} = \sqrt[5]{x^{-1}} = x^{-\frac{1}{5}}$.	11h \blacksquare	$\frac{x^2 \cdot \sqrt[3]{x}}{\sqrt{x}} = \frac{x^2 \cdot x^{\frac{1}{3}}}{x^{\frac{1}{2}}} = \frac{x^{2\frac{1}{3}}}{x^{\frac{1}{2}}} = x^{2\frac{1}{3}-\frac{1}{2}} = x^{\frac{5}{6}}$.		
12a	$8 \cdot \sqrt{2} = 2^3 \cdot 2^{\frac{1}{2}} = 2^{\frac{7}{2}}$.	12d	$\frac{4\sqrt{2}}{\sqrt[3]{2}} = \frac{2^2 \cdot 2^{\frac{1}{2}}}{2^{\frac{1}{3}}} = 2^{2\frac{1}{2}-\frac{1}{3}} = 2^{\frac{5}{6}}$.	12g	$\frac{1}{8} \cdot 3\sqrt{\frac{1}{4}} = 2^{-3} \cdot \sqrt[3]{2^{-2}} = 2^{-3} \cdot 2^{-\frac{2}{3}} = 2^{-3\frac{2}{3}}$.
12b	$\frac{8}{\sqrt{2}} = \frac{2^3}{2^{\frac{1}{2}}} = 2^{3-\frac{1}{2}} = 2^{2\frac{1}{2}}$.	12e	$4\sqrt{\frac{1}{9}} = \sqrt[4]{3^{-2}} = 3^{-\frac{2}{4}} = 3^{-\frac{1}{2}}$.	12h	$10 \cdot \sqrt[3]{0,1} = 10 \cdot \sqrt[3]{10^{-1}} = 10^1 \cdot 10^{-\frac{1}{3}} = 10^{\frac{2}{3}}$.
12c	$\frac{1}{2} \cdot \sqrt[3]{2} = 2^{-1} \cdot 2^{\frac{1}{3}} = 2^{-\frac{2}{3}}$.	12f	$\frac{1}{100} \sqrt{10} = 10^{-2} \cdot 10^{\frac{1}{2}} = 10^{-1\frac{1}{2}}$.		
13a	$x^{\frac{2}{3}} = x^2 \cdot x^{\frac{1}{3}} = x^2 \cdot \sqrt[3]{x}$.	13c	$2^{x+3} = 2^x \cdot 2^3 = 2^x \cdot 8 = 8 \cdot 2^x$.		
13b	$2^{\frac{2}{2}} = 2^2 \cdot 2^{\frac{1}{2}} = 4 \cdot \sqrt{2}$.	13d	$3^{x-2} = 3^x \cdot 3^{-2} = 3^x \cdot \frac{1}{9} = \frac{1}{9} \cdot 3^x$.		
14a	$1,18^{a+5} = 1,18^a \cdot 1,18^5 \approx 2,29 \cdot 1,18^a$.				
14b	$1,31^{a-2} = 1,31^a \cdot 1,31^{-2} \approx 0,58 \cdot 1,31^a$.				
14c	$0,78^{a+0,6} = 0,78^a \cdot 0,78^{0,6} \approx 0,86 \cdot 0,78^a$.				
14d	$1,15^{2a+1} = 1,15^{2a} \cdot 1,15^1 = (1,15^2)^a \cdot 1,15 \approx 1,15 \cdot 1,32^a$.				
14e	$1,22^{2a-1} = 1,22^{2a} \cdot 1,22^{-1} \approx (1,22^2)^a \cdot 0,82 \approx 0,82 \cdot 1,49^a$.				
14f	$8,35^{\frac{1}{3}a+0,4} = 8,35^{\frac{1}{3}a} \cdot 8,35^{0,4} \approx (8,35^{\frac{1}{3}})^a \cdot 2,34 \approx 2,34 \cdot 2,03^a$.				
14g	$8,35^{\frac{1}{3}a} = (8,35^{\frac{1}{3}})^a \approx 1,00 \cdot 2,03^a$.				
14h	$0,72^{2(a-1,2)} = 0,72^{2a-2,4} = 0,72^{2a} \cdot 0,72^{-2,4} \approx (0,72^2)^a \cdot 2,20 \approx 2,20 \cdot 0,52^a$.				
■					
15a \blacksquare	$x^{1,8} = 50$ $1.8 \times \sqrt{50}$ 8.787639344	15c \blacksquare	$3 \cdot x^{2,25} + 1 = 27$ $27-1$ $3 \cdot x^{2,25} = 26$ $x^{2,25} = \frac{26}{3}$ $x = \sqrt[2,25]{\frac{26}{3}} \approx 2,61$	15e \blacksquare	$4 \cdot x^{-1,8} + 16 = 500$ $500-16$ $4 \cdot x^{-1,8} = 484$ $x^{-1,8} = 121$ $x = \sqrt[1,8]{121} \approx 0,07$
	$x = \sqrt[1,8]{50} \approx 8,79$.		Ans/3 8.666666667 2.25 * Ans 2.611097882		484 Ans/4 121 .0696461344
15b \blacksquare	$x^{-3} = 5$ $(-3) \times \sqrt{5}$.5848035476	15d \blacksquare	$5 \cdot x^{-1} = 7$ $7/\sqrt{5}$ $x^{-1} = \frac{7}{5}$ $x = \sqrt[1/5]{7} \approx 0,71$	15f \blacksquare	$x^9 = \sqrt{3}$ $9 \times \sqrt{3}$ 1.06293507
	$x = \sqrt[3]{-5} \approx 0,58$.		(-1)¹ * sqrt(.4) .142857143		.5184 .0696461344
16a \blacksquare	$5 \cdot x^{-1,2} + 7 = 19$ $19-7$ Ans/5 (-1.2) * sqrt(2.4) .4821223875	16b \blacksquare	$4 \cdot x^{0,4} - 5 = 109$ $109+5$ Ans/4 0.4 * sqrt(28.5) 4336.228405	16c \blacksquare	$x^{\frac{1}{3}} = 10$ $(4/3) \times \sqrt{10}$ 5.623413252
	$5 \cdot x^{-1,2} = 12$ $x^{-1,2} = 2,4$ $x = \sqrt[1,2]{2,4} \approx 0,482$		12 28.5 4336.228405		$x = \sqrt[1/3]{10} \approx 5,623$

16d $\sqrt[3]{x^2} = 26$ 16e $5 \cdot \sqrt[3]{x} = 8$ 16f $3 \cdot \sqrt[4]{x^3} - 1 = 36$

$$\begin{array}{l} x^{\frac{2}{3}} = 26 \\ \sqrt[3]{x} = \sqrt[3]{26} \\ x = \sqrt[3]{26} \approx 132,575. \end{array}$$

$$\begin{array}{l} \sqrt[3]{x} = x^{\frac{1}{3}} = 1,6 \\ x = \sqrt[3]{1,6} = 4,096. \end{array}$$

$$\begin{array}{l} \sqrt[4]{x^3} = x^{\frac{3}{4}} = \frac{37}{3} \\ x = \sqrt[3]{\frac{37}{3}} \approx 28,495. \end{array}$$

17a $v = 67 - 50 = 17 \Rightarrow B = 20 + 0,7 \cdot 17^{1,52} \approx 72$ (€). ■

17b $20 + 0,7 \cdot v^{1,52} = 97$ 17c $20 + 0,7 \cdot v^{1,52} = 1648$ 17d Jeroen heeft geen gelijk.

$$\begin{array}{l} 0,7 \cdot v^{1,52} = 77 \\ v^{1,52} = 110 \\ v = \sqrt[1,52]{110} \approx 22. \end{array}$$

$$\begin{array}{l} 0,7 \cdot v^{1,52} = 1628 \\ v^{1,52} = \frac{1628}{0,7} \\ v = \sqrt[1,52]{\frac{1628}{0,7}} \approx 164. \end{array}$$

$$v = 5 \Rightarrow B = 20 + 0,7 \cdot 5^{1,52} \approx 28$$
 (€).
$$v = 10 \Rightarrow B = 20 + 0,7 \cdot 10^{1,52} \approx 43$$
 (€).

Er geldt $10 = 2 \cdot 5$, maar $43 \neq 2 \cdot 28$.

Ze reed $30 + 22 = 52$ km/u. ■ De snelheidsovertreding is 164 km/u. ■

18a $T = -20$ ($^{\circ}\text{C}$) en $v = 60$ (km/u) $\Rightarrow F = (2000 - 16,3 \cdot 60)(-5 - -20)^{-1,668} \approx 11$ (min). ■

18b $20 = (2000 - 16,3v)(-5 + 18)^{-1,668}$ 18c Met 40 km/u leg je 10 km af in 15 minuten.

$$\begin{array}{l} 2000 - 16,3v = \frac{20}{13^{-1,668}} \\ -16,3v \approx -557,5... \\ v \approx 34 \text{ km/u}. \end{array}$$

$$\begin{array}{l} 15 = (2000 - 16,3 \cdot 40)(-5 - T)^{-1,668} \\ (-5 - T)^{-1,668} = \frac{15}{2000 - 16,3 \cdot 40} \approx 0,011... \\ -5 - T \approx 14,832... \\ -T \approx 19,832... \Rightarrow T \approx -19,8$$
 ($^{\circ}\text{C}$). Dus voor $T \leq -20$ $^{\circ}\text{C}$. ■

19a $P = a \cdot Q^{2,5}$ en bij $Q = 3,2$ hoort $P = 8,1 \Rightarrow 8,1 = a \cdot 3,2^{2,5} \Rightarrow a = \frac{8,1}{3,2^{2,5}} \approx 0,44$. ■

19b $y = a \cdot \frac{1}{x^{1,81}}$ en bij $x = 12$ hoort $y = 16 \Rightarrow 16 = a \cdot \frac{1}{12^{1,81}} \Rightarrow a = 16 \cdot 12^{1,81} \approx 1437$. ■

20a $T = a \cdot R^{1,5}$ en bij $R = 12,20$ hoort $T = 15,9$ (Titan) $\Rightarrow 15,9 = a \cdot 12,20^{1,5} \Rightarrow a = \frac{15,9}{12,20^{1,5}} \approx 0,37$ ■

20b $R = 35,6 (\times 10^5 \text{ km}) \Rightarrow$ de omlooptijd is $T = 0,37 \cdot 35,6^{1,5} \approx 78,6$ dagen. ■

20c $T = \frac{15}{24} = 0,625$ (dagen) $\Rightarrow 0,625 = 0,37 \cdot R^{1,5} \Rightarrow \frac{0,625}{0,37} = R^{1,5} \Rightarrow R = \sqrt[1,5]{\frac{0,625}{0,37}} \approx 1,42 (\times 10^5 \text{ km})$. ■
De straal van de baan is ongeveer $1,42 \cdot 10^5$ km.

21a $W = a \cdot m^{0,75}$ en bij $m = 40$ hoort $W = 6700$ (schaap) $\Rightarrow 6700 = a \cdot 40^{0,75} \Rightarrow a = \frac{6700}{40^{0,75}} \approx 421$. ■

21b $m = 4$ (kg) $\Rightarrow W = 421 \cdot 4^{0,75} \approx 1191$ (kJ). ■

21c $W = 50000$ (kJ) $\Rightarrow 50000 = 421 \cdot m^{0,75} \Rightarrow \frac{50000}{421} = m^{0,75} \Rightarrow m = \sqrt[0,75]{\frac{50000}{421}} \approx 584$ (kg). ■

22ab Zie de plot hiernaast. De grafiek van f is stijgend.

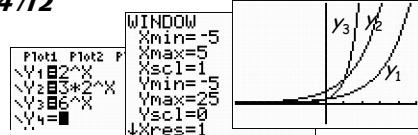
22c $f(-10) = 2^{-10} \approx 9,77 \cdot 10^{-4}$; $f(-20) = 2^{-20} \approx 9,54 \cdot 10^{-7}$
en $f(-100) = 2^{-100} \approx 7,89 \cdot 10^{-31}$.

22d $f(-500) = 2^{-500} = \frac{1}{2^{500}} > 0$. (De GR geeft $2^{-500} = 0$) ■

22e Voor elke x is $2^x > 0$, dus er is geen x (origineel) te vinden waarvoor $f(x) = 2^x$ (het beeld) = 0.



25a Zie de plot van de drie grafieken hiernaast.

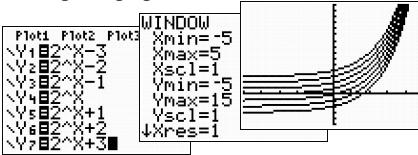


X	V1	V2	V3
-3	.125	.375	.00463
-2	.25	.75	.02778
-1	.5	1.5	.16667
0	1	3	.5
1	2	6	1.5
2	4	12	3
3	8	24	6

25b $y_1 = 2^x$ vermenigvuldigen met factor 3 $\rightarrow y_2 = 3 \cdot 2^x$.

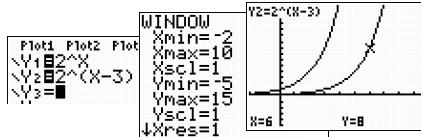
(dus de grafiek van y_2 ontstaat uit de grafiek van y_1 bij de vermenigvuldiging met 3)

26a Zie de plot van de grafieken hiernaast.



X	V1	V2	V3
-3	.125	.375	.00463
-2	.25	.75	.02778
-1	.5	1.5	.16667
0	1	3	.5
1	2	6	1.5
2	4	12	3
3	8	24	6

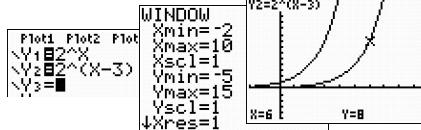
26b $y = 2^x$ 5 eenheden omhoog verschuiven $\rightarrow y = 2^x + 5$.



X	V1	V2
0	1	1.125
1	2	1.25
2	4	1.375
3	8	1.5
4	16	1.625
5	32	1.75
6	64	1.875

27a Zie de plot van de grafieken hiernaast.

$y = 2^x$ 3 naar rechts verschuiven $\rightarrow y = 2^{x-3}$.



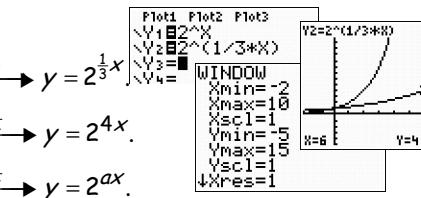
X	V1	V2
0	1	1.125
1	2	1.25
2	4	1.375
3	8	1.5
4	16	1.625
5	32	1.75
6	64	1.875

27b $y = 2^x$ 4 naar links verschuiven $\rightarrow y = 2^{x+4}$.

27c $y = 2^x$ b naar rechts verschuiven $\rightarrow y = 2^{x-b}$.

28a Zie de plot van de grafieken hiernaast.

28b $y = 2^x$ vermenigvuldiging t.o.v. de y-as met factor 3 $\rightarrow y = 2^{\frac{1}{3}x}$.



X	V1	V2
0	1	1.125
1	2	1.25
2	4	1.375
3	8	1.5
4	16	1.625
5	32	1.75
6	64	1.875

28c $y = 2^x$ vermenigvuldiging t.o.v. de y-as met factor $\frac{1}{4}$ $\rightarrow y = 2^{4x}$.

28d $y = 2^x$ vermenigvuldiging t.o.v. de y-as met factor $\frac{1}{a}$ $\rightarrow y = 2^{ax}$.

■

29a $y = 3^x$ met H.A.: de x-as ofwel $y = 0$

.....translatie (-2, 0)

$y = 3^{x+2}$ met H.A.: de x-as ofwel $y = 0$

.....translatie (0, -1)

$f(x) = 3^{x+2} - 1$ met H.A.: $y = -1$.

29b $y = 3^x$ met H.A.: de x-as ofwel $y = 0$

.....translatie (1, 0)

$y = 3^{x-1}$ met H.A.: de x-as ofwel $y = 0$

.....translatie (0, 5)

$g(x) = 3^{x-1} + 5$ met H.A.: $y = 5$.

29c $y = 0,5^x$ met H.A.: de x-as ofwel $y = 0$

.....vermenigvuldiging t.o.v. de x-as met 2

$y = 2 \cdot 0,5^x$ met H.A.: de x-as ofwel $y = 0$

.....translatie (0, 3)

$h(x) = 2 \cdot 0,5^x + 3$ met H.A.: $y = 3$.

30a $N = 1,5^t$ met B = $\langle 0, \rightarrow \rangle$ en H.A.: $N = 0$

.....vermenigvuldiging t.o.v. de t-as met 8

$N = 8 \cdot 1,5^t$ met B = $\langle 0, \rightarrow \rangle$ en H.A.: $N = 0$

.....translatie (0, -6)

$N = 8 \cdot 1,5^t - 6$ met B = $\langle -6, \rightarrow \rangle$ en H.A.: $N = -6$.

30b $N = 0,8^t$ met B = $\langle 0, \rightarrow \rangle$ en H.A.: $N = 0$

.....vermenigvuldiging t.o.v. de t-as met -2

$N = -2 \cdot 0,8^t$ met B = $\langle \leftarrow, 0 \rangle$ en H.A.: $N = 0$

.....translatie (0, 5)

$N = -2 \cdot 0,8^t + 5$ met B = $\langle \leftarrow, 5 \rangle$ en H.A.: $N = 5$.

29d $y = 0,7^x$ met H.A.: de x-as ofwel $y = 0$

.....vermenigvuldiging t.o.v. de x-as met -3

$y = -3 \cdot 0,7^x$ met H.A.: de x-as ofwel $y = 0$

.....translatie (0, 5)

$k(x) = -3 \cdot 0,7^x + 5$ met H.A.: $y = 5$.

29e $y = 2^x$ met H.A.: de x-as ofwel $y = 0$

.....vermenigvuldiging t.o.v. de x-as met 3

$y = 3 \cdot 2^x$ met H.A.: de x-as ofwel $y = 0$

.....vermenigvuldiging t.o.v. de y-as met $\frac{1}{3}$

$y = 3 \cdot 2^{3x}$ met H.A.: de x-as ofwel $y = 0$

.....translatie (0, 4)

$l(x) = 3 \cdot 2^{3x} + 4$ met H.A.: $y = 4$.

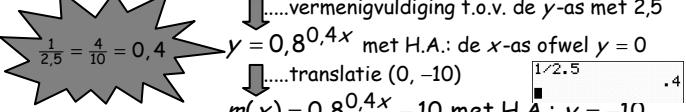
29f $y = 0,8^x$ met H.A.: de x-as ofwel $y = 0$

.....vermenigvuldiging t.o.v. de y-as met 2,5

$y = 0,8^{0,4x}$ met H.A.: de x-as ofwel $y = 0$

.....translatie (0, -10)

$m(x) = 0,8^{0,4x} - 10$ met H.A.: $y = -10$.



30c $N = 0,3^t$ met B = $\langle 0, \rightarrow \rangle$ en H.A.: $N = 0$

.....verm. t.o.v. de t-as met -1

$N = -0,3^t$ met B = $\langle \leftarrow, 0 \rangle$ en H.A.: $N = 0$

.....translatie (1, 0)

$N = -0,3^{t-1}$ met B = $\langle \leftarrow, 0 \rangle$ en H.A.: $N = 0$

.....translatie (0, 1000)

$N = 1000 - 0,3^{t-1}$ met B = $\langle \leftarrow, 1000 \rangle$ en H.A.: $N = 1000$.

30d $N = 0,3^t$ met B = $\langle 0, \rightarrow \rangle$ en H.A.: $N = 0$

.....verm. t.o.v. de t-as met -1

$N = -0,3^t$ met B = $\langle \leftarrow, 0 \rangle$ en H.A.: $N = 0$

.....translatie (0, 1)

$N = 1 - 0,3^t$ met B = $\langle \leftarrow, 1 \rangle$ en H.A.: $N = 1$

.....vermenigvuldiging t.o.v. de t-as met 1000

$N = 1000(1 - 0,3^t)$ met B = $\langle \leftarrow, 1000 \rangle$ en H.A.: $N = 1000$.

31a $y = 3^x$
 ↓verm. t.o.v. de x -as met $\frac{1}{2}$
 $y = \frac{1}{2} \cdot 3^x$
 ↓translatie (0, 3)
 $f(x) = \frac{1}{2} \cdot 3^x + 3.$

31b $y = 3^x$
 ↓verm. t.o.v. de x -as met -1
 $y = -3^x$
 ↓translatie (0, -1)
 $g(x) = -3^x - 1.$

31c $y = 3^x$
 ↓translatie (0, -5)
 $y = 3^x - 5$
 ↓translatie (4, 0)
 $y = 3^{x-4} - 5$
 ↓verm. t.o.v. de x -as met 3
 $h(x) = 3 \cdot (3^{x-4} - 5) = 3 \cdot 3^{x-4} - 15.$

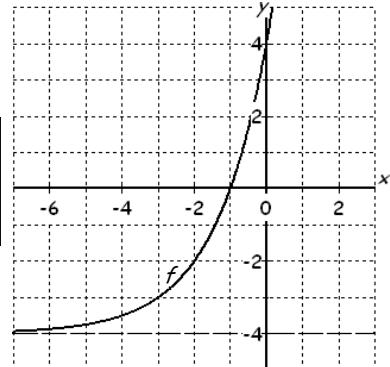
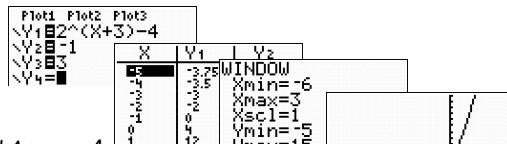
31d $y = 3^x$
 ↓verm. t.o.v. de x -as met 3
 $y = 3 \cdot 3^x$
 ↓translatie (0, -5)
 $y = 3 \cdot 3^x - 5$
 ↓translatie (4, 0)
 $k(x) = 3 \cdot 3^{x-4} - 5.$

32 □ *

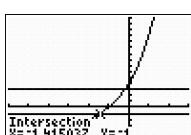
33 □ *

34 □ *

35ab $y = 2^x$ met $B = \langle 0, \rightarrow \rangle$ en H.A.: $y = 0$
 ↓translatie (-3, 0)
 $y = 2^{x+3}$ met $B = \langle 0, \rightarrow \rangle$ en H.A.: $y = 0$
 ↓translatie (0, -4)
 $f(x) = 2^{x+3} - 4$ met $B_f = \langle -4, \rightarrow \rangle$ en H.A.: $y = -4$.
 (neem de tabel over van de GR en teken de grafiek)

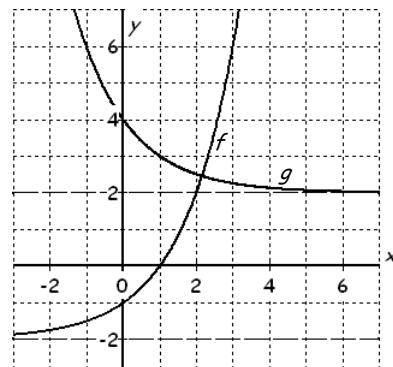
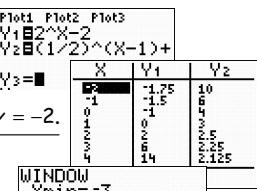


35c $f(x) = 2^{x+3} - 4 = -1$ (intersect) $\Rightarrow x \approx -1,42.$
 $f(x) \leq -1$ (zie plot/grafiek) $\Rightarrow x \leq -1,42.$

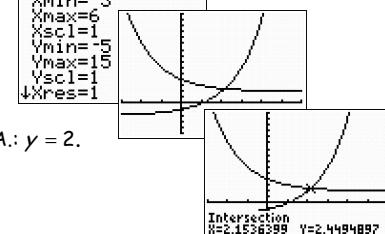


35d $f(3) = 2^6 - 4 = 64 - 4 = 60.$
 $x \leq 3$ (zie plot/grafiek en B_f) $\Rightarrow -4 < f(x) \leq 60.$

36ab $y = 2^x$ met $B = \langle 0, \rightarrow \rangle$ en H.A.: $y = 0$
 ↓translatie (0, -2)
 $f(x) = 2^x - 2$ met $B_f = \langle -2, \rightarrow \rangle$ en H.A.: $y = -2.$



$y = \left(\frac{1}{2}\right)^x$ met $B = \langle 0, \rightarrow \rangle$ en H.A.: $y = 0$
 ↓translatie (1, 0)
 $y = \left(\frac{1}{2}\right)^{x-1}$ met $B = \langle 0, \rightarrow \rangle$ en H.A.: $y = 0$
 ↓translatie (0, 2)

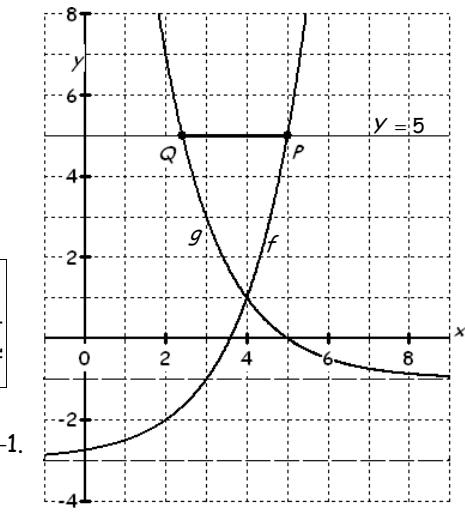
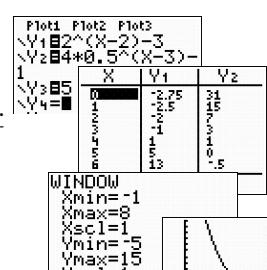


$g(x) = \left(\frac{1}{2}\right)^{x-1} + 2$ met $B_g = \langle 2, \rightarrow \rangle$ en H.A.: $y = 2.$

36c $f(x) = g(x)$ (intersect) $\Rightarrow x \approx 2,15.$
 $f(x) \geq g(x)$ (zie grafiek) $\Rightarrow x \geq 2,15.$

36d $B_f = \langle -2, \rightarrow \rangle \Rightarrow f(x) = p$ heeft geen oplossingen voor $p \leq -2.$

37a $y = 2^x$ met $B = \langle 0, \rightarrow \rangle$ en H.A.: $y = 0$
 ↓translatie (2, -3)



$f(x) = 2^{x-2} - 3$ met $B_f = \langle -3, \rightarrow \rangle$ en H.A.: $y = -3.$

$y = 0,5^x$ met $B = \langle 0, \rightarrow \rangle$ en H.A.: $y = 0$

↓verm. t.o.v. de x -as met 4

$y = 4 \cdot 0,5^x$ met $B = \langle 0, \rightarrow \rangle$ en H.A.: $y = 0$

↓translatie (3, -1)

$g(x) = 4 \cdot 0,5^{x-3} - 1$ met $B = \langle -1, \rightarrow \rangle$ en H.A.: $y = -1.$

37b $B_f = \langle -3, \rightarrow \rangle \Rightarrow f(x) = p$ heeft één oplossing voor $p > -3.$

$B_g = \langle -1, \rightarrow \rangle \Rightarrow g(x) = p$ heeft geen oplossing voor $p \leq -1.$

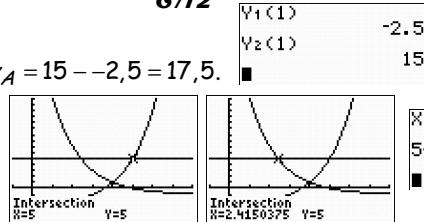
$f(x) = p$ heeft één oplossing én $g(x) = p$ heeft geen oplossing $\Rightarrow -3 < p \leq -1.$

37c $f(2) = 2^0 - 3 = 1 - 3 = -2.$

$x \leq 2$ (zie plot/grafiek en B_f) $\Rightarrow -3 < f(x) \leq -2.$

37d $f(1) = -2,5$ en $g(1) = 15 \Rightarrow AB = y_B - y_A = 15 - -2,5 = 17,5.$

37e $f(x) = 5$ (intersect) $\Rightarrow x = x_P = 5$ en
 $g(x) = 5$ (intersect) $\Rightarrow x = x_Q \approx 2,415.$
 $PQ = x_P - x_Q \approx 5 - 2,415 = 2,585.$



38a $f(x) = 2^{x-3} = \sqrt{2}$
aflezen in de grafiek:
 $x \approx 3,5.$

38b $2^{x-3} = \sqrt{2} = 2^{\frac{1}{2}}$
 $x-3 = \frac{1}{2}$
 $x = 3\frac{1}{2}.$

X	Y ₁	Y ₂
0	1	1
1	2	2
2	4	4
3	8	8
4	16	16
5	32	32
6	64	64
7	128	128
8	256	256
9	512	512
10	1024	1024
11	2048	2048
12	4096	4096
13	8192	8192
14	16384	16384
15	32768	32768
16	65536	65536
17	131072	131072
18	262144	262144
19	524288	524288
20	1048576	1048576

39a $2^{x+1} = 64 = 2^6$
 $x+1 = 6$
 $x = 5.$

39d $2^x = 1 = 2^0$
 $x = 0.$

39g $5^{x+6} = \left(\frac{1}{5}\right)^x = (5^{-1})^x = 5^{-x}$
 $x+6 = -x$
 $2x = -6 \Rightarrow x = -3.$

39b $2^{x-3} = \frac{1}{8} = \frac{1}{2^3} = 2^{-3}$
 $x-3 = -3$
 $x = 0.$

39e $2^x = \frac{1}{4}\sqrt{2} = \frac{1}{2^2} \cdot 2^{\frac{1}{2}} = 2^{-2} \cdot 2^{\frac{1}{2}} = 2^{-\frac{3}{2}}$
 $x = -1\frac{1}{2}.$

39h $3^{2x+1} = 27\sqrt{3} = 3^3 \cdot 3^{\frac{1}{2}} = 3^{\frac{7}{2}}$
 $2x+1 = 3\frac{1}{2}$
 $2x = 2\frac{1}{2} \Rightarrow x = 1\frac{1}{4}.$

39c $2^{2x} = 2 = 2^1$
 $2x = 1$
 $x = \frac{1}{2}.$

39f $2^{x+5} = 16\sqrt{2} = 2^4 \cdot 2^{\frac{1}{2}} = 2^{4\frac{1}{2}}$
 $x+5 = 4\frac{1}{2}$
 $x = -\frac{1}{2}.$

39i $10^{2x+1} = 0,01 = \frac{1}{100} = \frac{1}{10^2} = 10^{-2}$
 $2x+1 = -2$
 $2x = -3 \Rightarrow x = -1\frac{1}{2}.$

40a $2^x + 1 = 17$
 $2^x = 16 = 2^4$
 $x = 4.$

40d $10 \cdot 3^x = 270$
 $3^x = 27 = 3^3$
 $x = 3.$

40g $5^{2x-6} = 0,04 = \frac{4}{100} = \frac{1}{25} = \frac{1}{5^2} = 5^{-2}$
 $2x-6 = -2$
 $2x = 4 \Rightarrow x = 2.$

40b $3^x - 2 = 25$
 $3^x = 27 = 3^3$
 $x = 3.$

40e $3 \cdot 8^{2-x} = 48$
 $8^{2-x} = 16 = 2^4$
 $(2^3)^{2-x} = 2^{6-3x} = 2^4$
 $6-3x = 4 \Rightarrow -3x = -2 \Rightarrow x = \frac{2}{3}.$

40h $3 \cdot 7^{3x+1} = 147 \quad \boxed{147/3}$
 $7^{3x+1} = 49 = 7^2 \quad \boxed{49}$
 $3x+1 = 2$
 $3x = 1 \Rightarrow x = \frac{1}{3}.$

40c $5 \cdot 2^x = 80$
 $2^x = 16 = 2^4 \quad \boxed{80/5}$
 $x = 4.$

40f $3 \cdot 2^x + 4 = 28$
 $3 \cdot 2^x = 24$
 $2^x = 8 = 2^3$
 $x = 3.$

40i $32^{x-2} = \frac{1}{16}$
 $(2^5)^{x-2} = \frac{1}{2^4}$
 $2^{5x-10} = 2^{-4}$
 $5x-10 = -4 \Rightarrow 5x = 6 \Rightarrow x = \frac{6}{5}.$

41a Zie de grafieken hiernaast. (gebruikt een tabel)

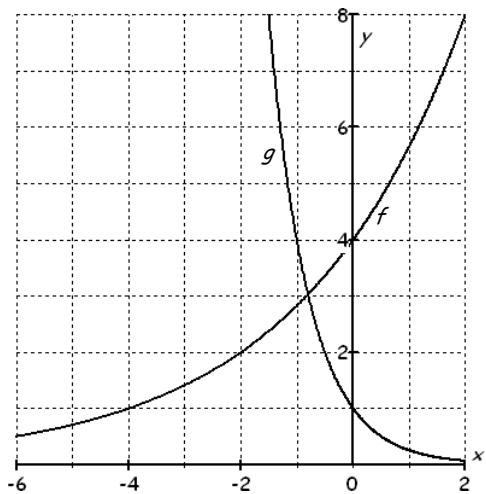
X	Y ₁	Y ₂
-2	8	16
-1	2.8284	4
0	1	1
1	5.6569	25
2	11.314	.0625
3	16	.00256

41b $f(x) = g(x)$
 $(\sqrt{2})^{x+4} = \left(\frac{1}{4}\right)^x$
 $\left(2^{\frac{1}{2}}\right)^{x+4} = \left(\frac{1}{2^2}\right)^x$
 $2^{\frac{1}{2}(x+4)} = (2^{-2})^x$
 $2^{\frac{1}{2}x+2} = 2^{-2x}$
 $\frac{1}{2}x+2 = -2x$
 $2\frac{1}{2}x = -2$
 $x = \frac{-2}{2.5} = \frac{-4}{5} = -\frac{4}{5}.$

Lees af in de grafiek: $f(x) \geq g(x) \Rightarrow x \geq -\frac{4}{5}.$

41c $g(x) = \sqrt{2}$
 $\left(\frac{1}{4}\right)^x = \sqrt{2}$
 $2^{-2x} = 2^{\frac{1}{2}}$
 $-2x = \frac{1}{2}$
 $x = -\frac{1}{4}.$

Lees af: $g(x) \geq \sqrt{2} \Rightarrow x \leq -\frac{1}{4}.$



42a $x \begin{array}{|c|} \hline \times 3 \\ \hline \end{array} 5$ heeft als omkeerschema

$x \begin{array}{|c|} \hline :3 \\ \hline \end{array} 5$

42b $x \begin{array}{|c|} \hline \sqrt[3]{...} \\ \hline \end{array} 5$ heeft als omkeerschema

$x \begin{array}{|c|} \hline \sqrt[3]{...} \\ \hline \end{array} 5$

- 43a $2^x = 3$ heffen elkaar op
 $x = 2 \log(3)$.
 $2^x = 3$ (intersect) $\Rightarrow x \approx 1,58$.
- 43b $\left(\frac{1}{2}\right)^x = 7$ heffen elkaar op
 $x = \frac{1}{2} \log(7)$.
 $\left(\frac{1}{2}\right)^x = 7$ (intersect) $\Rightarrow x \approx -2,81$.
- 44a $2^x = 5$ (intersect) $\Rightarrow x = 2 \log(5) \approx 2,32$.
- 44b $4^x = 0,6$ (intersect) $\Rightarrow x = 4 \log(0,6) \approx -0,37$.
- 45a $2^{x-1} = 15$ ($2 \log$... nemen)
 $x-1 = 2 \log(15)$
 $x = 2 \log(15) + 1$.
- 45c $4 + 3^{x+1} = 25$
 $3^{x+1} = 21$ ($3 \log$... nemen)
 $x+1 = 3 \log(21)$
 $x = 3 \log(21) - 1$.
- 45d $14 - 2^{x+1} = 2$
 $-2^{x+1} = -12$
 $2^{x+1} = 12$ ($2 \log$... nemen)
 $x+1 = 2 \log(12)$
 $x = 2 \log(12) - 1$.
- 45e $7 + 4^{2x} = 12$
 $4^{2x} = 5$ ($4 \log$... nemen)
 $2x = 4 \log(5)$
 $x = \frac{1}{2} \cdot 4 \log(5)$.
- 45f $3 \cdot 5^{2x+1} = 60$
 $5^{2x+1} = 20$ ($5 \log$... nemen)
 $2x+1 = 5 \log(20)$
 $2x = 5 \log(20) - 1$
 $x = \frac{1}{2} \cdot 5 \log(20) - \frac{1}{2}$.
- 46 $2^x = 32$ heeft als oplossing $x = 2 \log(32)$
 $2^x = 32 = 2^5$ heeft als oplossing $x = 5$ $\Rightarrow 2 \log(32) = 5$ of $2 \log(32) = 2 \log(2^5) = 5$
- 47a $2 \log(4) = 2 \log(2^2) = 2$.
- 47b $2 \log(2) = 2 \log(2^1) = 1$.
- 47c $2 \log\left(\frac{1}{2}\right) = 2 \log(2^{-1}) = -1$.
- 47d $2 \log(\sqrt{2}) = 2 \log(2^{\frac{1}{2}}) = \frac{1}{2}$.
- 47e $2 \log\left(\frac{1}{4}\right) = 2 \log\left(\frac{1}{2^2}\right) = 2 \log(2^{-2}) = -2$.
- 47f $2 \log(1) = 2 \log(2^0) = 0$.
- 47g $2 \log(4 \cdot \sqrt{2}) = 2 \log(2^2 \cdot 2^{\frac{1}{2}}) = 2 \log(2^{\frac{5}{2}}) = 2\frac{1}{2}$.
- 47h $2 \log\left(\frac{1}{8} \cdot \sqrt{2}\right) = 2 \log\left(\frac{1}{2^3} \cdot 2^{\frac{1}{2}}\right) = 2 \log(2^{-3} \cdot 2^{\frac{1}{2}}) = 2 \log(2^{-2\frac{1}{2}}) = -2\frac{1}{2}$.
- 48a $3 \log(27) = 3 \log(3^3) = 3$.
- 48b $7 \log(49) = 7 \log(7^2) = 2$.
- 48c $3 \log\left(\frac{1}{81}\right) = 3 \log\left(\frac{1}{3^4}\right) = 3 \log(3^{-4}) = -4$.
- 48d $10 \log(1000) = 10 \log(10^3) = 3$.
- 48e $10 \log(0,01) = 10 \log\left(\frac{1}{100}\right) = 10 \log\left(\frac{1}{10^2}\right) = 10 \log(10^{-2}) = -2$.
- 48f $10 \log(0,1 \cdot \sqrt{10}) = 10 \log\left(\frac{1}{10} \cdot 10^{\frac{1}{2}}\right) = 10 \log(10^{-1} \cdot 10^{\frac{1}{2}}) = 10 \log(10^{-\frac{1}{2}}) = -\frac{1}{2}$.
- 48g $7 \log(1) = 7 \log(7^0) = 0$.
- 48h $23 \log(23) = 23 \log(23^1) = 1$.
- 49a $5 \log(0,2) = 5 \log\left(\frac{2}{10}\right) = 5 \log\left(\frac{1}{5}\right) = 5 \log(5^{-1}) = -1$.
- 49b $3 \log(3 \cdot \sqrt{3}) = 3 \log(3^1 \cdot 3^{\frac{1}{2}}) = 3 \log(3^{\frac{3}{2}}) = 1\frac{1}{2}$.
- 49c $\frac{1}{2} \log(8) = \frac{1}{2} \log\left(\left(\frac{1}{2}\right)^{-3}\right) = -3$.
- 49d $\frac{1}{4} \log\left(\frac{1}{16}\right) = \frac{1}{4} \log\left(\left(\frac{1}{4}\right)^2\right) = 2$.
- 49e $0,25 \log(4) = \frac{1}{4} \log(4) = \frac{1}{4} \log\left(\left(\frac{1}{4}\right)^{-1}\right) = -1$.
- 49f $4 \log(0,25) = 4 \log\left(\frac{1}{4}\right) = 4 \log(4^{-1}) = -1$.
- 49g $\frac{1}{7} \log(7) = \frac{1}{7} \log\left(\left(\frac{1}{7}\right)^{-1}\right) = -1$.
- 49h $\frac{1}{7} \log(1) = \frac{1}{7} \log\left(\left(\frac{1}{7}\right)^0\right) = 0$.
- 50a $2 \log(x) = 8$ (2^{...} nemen)
 $x = 2^8 = 256$.
- 50c $x \log(3) = 1$ (x^{...} nemen)
 $3 = x^1$ (dus $x = 3$).
- 50d $2 \log(x+3) = -1$ (2^{...} nemen)
 $x+3 = 2^{-1} = \frac{1}{2}$
 $x = -2\frac{1}{2}$.
- 50e $\frac{1}{2} \log\left(x - \frac{1}{2}\right) = -1$ (($\frac{1}{2}$)^{...} nemen)
 $x - \frac{1}{2} = \left(\frac{1}{2}\right)^{-1} = 2$
 $x = 2\frac{1}{2}$.
- 50f $3 \log(x^2 + 1) = 2$ (3^{...} nemen)
 $x^2 + 1 = 3^2 = 9$
 $x^2 = 8$
 $x = -\sqrt{8} \vee x = \sqrt{8}$.

51ab Zie de tabel hieronder.

x	$\frac{1}{8}$	$\frac{1}{4}$	$\frac{1}{2}$	1	2	4	8
$f(x) = {}^2\log(x)$	-3	-2	-1	0	1	2	3

Zie de grafiek hiernaast.

51c Bij ${}^2\log(x)$ moet x (een macht van 2) > 0 zijn $\Rightarrow D_f = \langle 0, \rightarrow \rangle$.

51d $B_f = \mathbb{R}$.

■

52a $y = {}^3\log(x)$ met V.A.: de y -as ($x = 0$)

\downarrow translatie $(-2, 0)$

$f(x) = {}^3\log(x+2)$ met V.A.: $x = -2$.

52d $y = {}^{\frac{1}{3}}\log(x)$ met V.A.: de y -as ($x = 0$)

\downarrow verm. t.o.v. de x -as met -1

$y = -{}^{\frac{1}{3}}\log(x)$ met V.A.: $x = 0$

\downarrow translatie $(-1, -2)$

$k(x) = -{}^{\frac{1}{3}}\log(x+1) - 2$ met V.A.: $x = -1$.

52b $y = {}^2\log(x)$ met V.A.: de y -as ($x = 0$)

\downarrow verm. t.o.v. de x -as met 5

$y = 5 \cdot {}^2\log(x)$ met V.A.: $x = 0$

\downarrow translatie $(1, 0)$

$g(x) = 5 \cdot {}^2\log(x-1)$ met V.A.: $x = 1$.

52e $y = {}^3\log(x)$ met V.A.: de y -as ($x = 0$)

\downarrow verm. t.o.v. de y -as met $\frac{1}{2}$

$y = {}^3\log(2x)$ met V.A.: $x = 0$

\downarrow translatie $(0, 5)$

$l(x) = {}^3\log(2x) + 5$ met V.A.: $x = 0$.

52c $y = {}^{\frac{1}{2}}\log(x)$ met V.A.: de y -as ($x = 0$)

\downarrow verm. t.o.v. de x -as met 4

$y = 4 \cdot {}^{\frac{1}{2}}\log(x)$ met V.A.: $x = 0$

\downarrow translatie $(0, 3)$

$h(x) = 4 \cdot {}^{\frac{1}{2}}\log(x) + 3$ met V.A.: $x = 0$.

52f $y = {}^{\frac{1}{4}}\log(x)$ met V.A.: de y -as ($x = 0$)

\downarrow verm. t.o.v. de x -as met 3

$y = 3 \cdot {}^{\frac{1}{4}}\log(x)$ met V.A.: $x = 0$

\downarrow verm. t.o.v. de y -as met 2

$m(x) = 3 \cdot {}^{\frac{1}{4}}\log(\frac{1}{2}x)$ met V.A.: $x = 0$.

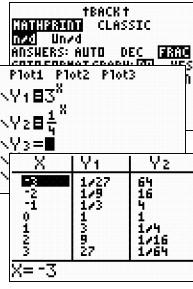
53a $y = {}^3\log(x)$ met V.A.: de y -as ($x = 0$)

\downarrow translatie $(4, 2)$

$f(x) = {}^3\log(x-4) + 2$ met V.A.: $x = 4$.

53b $D_f = \langle 4, \rightarrow \rangle$. Maak de tabel hieronder en de grafiek hiernaast.
(gebruik de tabel op de GR hiernaast)

x	$\frac{1}{9}$	$\frac{1}{3}$	1	3	9
$y = {}^3\log(x)$	-2	-1	0	1	2



54a $y = {}^{\frac{1}{4}}\log(x)$ met V.A.: de y -as ($x = 0$)

\downarrow translatie $(3, 2)$

$f(x) = {}^{\frac{1}{4}}\log(x-3) + 2$ met V.A.: $x = 3$.

54b $D_f = \langle 3, \rightarrow \rangle$. Maak de tabel hieronder en de grafiek hiernaast.
(zie het TABLE-scherm van de GR naast 53b)

x	16	4	1	$\frac{1}{4}$	$\frac{1}{16}$
$y = {}^{\frac{1}{4}}\log(x)$	-2	-1	0	1	2



55a $y = {}^3\log(x)$

\downarrow verm. t.o.v. de x -as met 2

$y = 2 \cdot {}^3\log(x)$

\downarrow translatie $(0, -4)$

$f(x) = 2 \cdot {}^3\log(x) - 4$.

55b

$y = {}^3\log(x)$

\downarrow spiegelen in de x -as

$y = -{}^3\log(x)$

\downarrow translatie $(5, 0)$

$g(x) = -{}^3\log(x-5)$.

55c

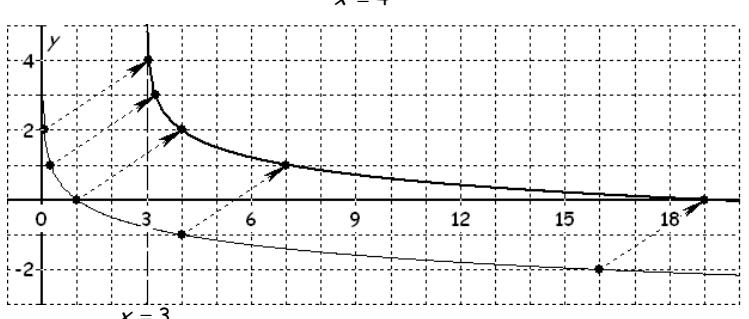
$y = {}^3\log(x)$

\downarrow translatie $(-3, 2)$

$y = {}^3\log(x+3) + 2$

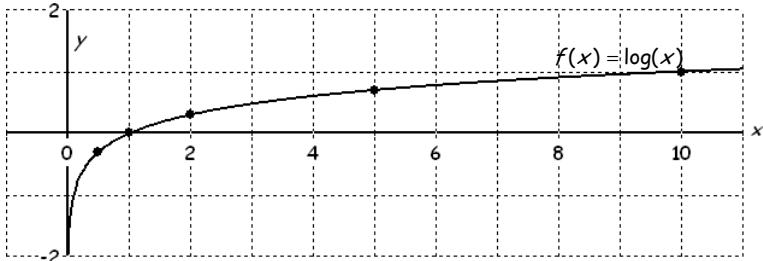
\downarrow verm. t.o.v. de x -as met $\frac{1}{2}$

$h(x) = \frac{1}{2} \cdot ({}^3\log(x+3) + 2)$
 $= \frac{1}{2} \cdot {}^3\log(x+3) + 1$.



56a Vul de tabel verder. (zie de GR-schermen hieronder)

$\log(1/2)$	$\log(5)$
-0,3010299957	0,6989700043
$\log(1)$	0
$\log(2)$	1



56b Zie de grafiek hiernaast.

56c $X_{\min} = 0$, $X_{\max} = 10$, $Y_{\min} = -1$ en $Y_{\max} = 1$.

57a $\text{din} = 1 + k \cdot \log(\text{iso})$ met $100 \text{ ISO} = 21 \text{ DIN} \Rightarrow 21 = 1 + k \cdot \log(100) \Rightarrow 20 = k \cdot \log(10^2) \Rightarrow 20 = k \cdot 2 \Rightarrow k = \frac{20}{2} = 10$.

57b $400 \text{ ISO/ASA} \Rightarrow \text{din} = 1 + 10 \cdot \log(400) \approx 27$. Dus 27 DIN .

57c $24 \text{ DIN} \Rightarrow 24 = 1 + 10 \cdot \log(\text{iso}) \Rightarrow 23 = 10 \cdot \log(\text{iso}) \Rightarrow 2,3 = \log(\text{iso}) \Rightarrow \text{iso} = 10^{2,3} \approx 200$. Dus 200 ISO/ASA .

Diagnostische toets

D1a $6a^3 \cdot 8(a^2)^2 = 6a^3 \cdot 8a^4 = 48a^7$.

D1b $(6a)^3 \cdot (8a^2)^2 = 216a^3 \cdot 64a^4 = 13824a^7$.

D1c $\frac{(6a^2)^3}{(2a)^4} = \frac{216a^6}{16a^4} = 13\frac{1}{2}a^2$.

6^3
 $Ans \cdot 8^2$

216
 13824

D1d $(2a^2)^4 - (3a^3)^2 = 16a^8 - 9a^6$.

D1e $(ab^2)^4 \cdot a^2b = a^4b^8 \cdot a^2b = a^6b^9$.

D1f $\left(\frac{6a^2}{2a}\right)^4 = (3a)^4 = 81a^4$.

D2a $a^{-3} \cdot a^2 = a^{-3+2} = a^{-1}$.

D2b $(a^{-3})^2 = a^{-3 \cdot 2} = a^{-6}$.

D2c $\frac{a^{-3}}{a^2} = a^{-3-2} = a^{-5}$.

D3a $a^{-2} = \frac{1}{a^2}$.

D3b $10ab^{-2} = \frac{10a}{b^2}$.

D3c $(4a)^{-2} \cdot 3b^{-4} = \frac{1}{(4a)^2} \cdot \frac{3}{b^4} = \frac{3}{16a^2b^4}$.

D4a $3\frac{1}{2}a^{\frac{2}{7}} = 3\frac{1}{2} \cdot \sqrt[7]{a^2}$.

D4b $2a^{-3}b^{\frac{1}{3}} = 2 \cdot \frac{1}{a^3} \cdot \sqrt[3]{b} = \frac{2 \cdot \sqrt[3]{b}}{a^3}$.

D4c $4a^{\frac{1}{4}}b^{-\frac{2}{3}} = 4 \cdot \sqrt[4]{a} \cdot \frac{1}{\sqrt[3]{b^2}} = 4 \cdot \sqrt[4]{a} \cdot \frac{1}{\sqrt[3]{b^2}} = \frac{4 \cdot \sqrt[4]{a}}{\sqrt[3]{b^2}}$.

D5a $\frac{1}{x^3} = x^{-3}$.

D5d $x^3 \cdot \sqrt[5]{x^3} = x^3 \cdot x^{\frac{3}{5}} = x^{3+\frac{3}{5}} = x^{\frac{18}{5}}$.

D5b $\frac{1}{x^2 \cdot \sqrt{x}} = \frac{1}{x^2 \cdot x^{\frac{1}{2}}} = \frac{1}{x^{\frac{5}{2}}} = x^{-\frac{5}{2}}$.

D5e $\frac{x^4}{\sqrt[3]{x}} = \frac{x^4}{x^{\frac{1}{3}}} = x^4 \cdot x^{-\frac{1}{3}} = x^{\frac{11}{3}}$.

D5c $\sqrt[3]{x^2} = x^{\frac{2}{3}}$.

D5f $\sqrt[3]{\frac{1}{x^3}} = \sqrt[3]{x^{-3}} = x^{-\frac{3}{3}} = x^{-1}$.

D6a $16 \cdot \sqrt{2} = 2^4 \cdot 2^{\frac{1}{2}} = 2^{\frac{9}{2}}$.

$\sqrt[3]{32} = \sqrt[3]{2^5} = 2^{\frac{5}{3}} = 2^{\frac{12}{9}}$.

$\sqrt[5]{\frac{1}{8}} = \sqrt[5]{\frac{1}{2^3}} = \sqrt[5]{2^{-3}} = 2^{-\frac{3}{5}}$.

D6b $2^{x-4} = 2^x \cdot 2^{-4} = 2^x \cdot \frac{1}{16} = \frac{1}{16} \cdot 2^x$.

$2^{x+\frac{1}{2}} = 2^x \cdot 2^{\frac{1}{2}} = 2^x \cdot \sqrt{2} = \sqrt{2} \cdot 2^x$.

D6c $2,16^{a-1} = 2,16^a \cdot 2,16^{-1} \approx 0,46 \cdot 2,16^a$.

$2.16^{-1} \cdot 462962963$

$1,27^{3a+0,6} = 1,27^{3a} \cdot 1,27^{0,6} \approx 1,15 \cdot (1,27^3)^a \approx 1,15 \cdot 2,05^a$.

D7a $5x^{1,2} + 6 = 20$.

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$5x^{1,2} = 14$
 $x^{1,2} = 2,8$
 $x = \sqrt[1,2]{2,8} \approx 2,358$

D7b $6 \cdot \sqrt[3]{x^2} + 3 = 8$

$6 \cdot \sqrt[3]{x^2} = 5$
 $x^{\frac{2}{3}} = \frac{5}{6}$
 $x = \sqrt[3]{\frac{5}{6}} \approx 0,761$

D7c $8x \cdot \sqrt{x} + 5 = 21$

$8x^{\frac{1}{2}} \cdot x^{\frac{1}{2}} = 16$
 $x^{\frac{11}{2}} = 2$
 $x = \sqrt[11]{2} \approx 1,587$

X	Y1
0	1
1	2
2	4
3	8
4	16
5	32
6	64

Plot1 Plot2
 $\checkmark Y_1 = 2^x$
 $\checkmark Y_2 =$
 $\checkmark Y_3 =$

$X=0$

D8a $K = a \cdot p^{1,3}$ en bij $p=17$ hoort $K=150 \Rightarrow 150 = a \cdot 17^{1,3} \Rightarrow a = \frac{150}{17^{1,3}} \approx 3,77$.

D8b $N = \frac{a}{t^{0,83}}$ en bij $t=11$ hoort $N=33 \Rightarrow 33 = \frac{a}{11^{0,83}} \Rightarrow a = 33 \cdot 11^{0,83} \approx 241$.

D9a $N = 0,9^t$ met $B = \langle 0, \rightarrow \rangle$ en H.A.: $N=0$

↓....verm. t.o.v. de t-as met -1

$N = -0,9^t$ met $B = \langle \leftarrow, 0 \rangle$ en H.A.: $N=0$

↓....translatie (0, 800)

$N = 800 - 0,9^t$ met $B = \langle \leftarrow, 800 \rangle$ en H.A.: $N=800$.

D9b $N = 1,2^t$ met $B = \langle 0, \rightarrow \rangle$ en H.A.: $N=0$

↓....verm. t.o.v. de t-as met 0,5

$N = 0,5 \cdot 1,2^t$ met $B = \langle 0, \rightarrow \rangle$ en H.A.: $N=0$

↓....translatie (0, 3)

$N = 0,5 \cdot 1,2^t + 3$ met $B = \langle 3, \rightarrow \rangle$ en H.A.: $N=3$.

D10ab \square Zie de grafieken hiernaast. (gebruikt een tabel)

$$y = 3^x \text{ met } B = \langle 0, \rightarrow \rangle \text{ en H.A.: } y = 0$$

\downarrow translatie $(2, -3)$

$$f(x) = 3^{x-2} - 3 \text{ met } B_f = \langle -3, \rightarrow \rangle \text{ en H.A.: } y = -3.$$

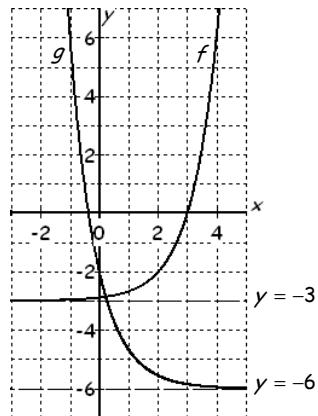
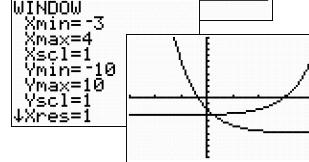
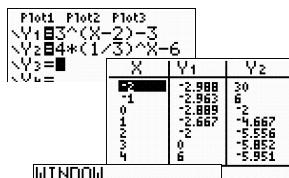
$$y = \left(\frac{1}{3}\right)^x \text{ met } B = \langle 0, \rightarrow \rangle \text{ en H.A.: } y = 0$$

\downarrow verm. t.o.v. de x -as met 4

$$y = 4 \cdot \left(\frac{1}{3}\right)^x \text{ met } B = \langle 0, \rightarrow \rangle \text{ en H.A.: } y = 0$$

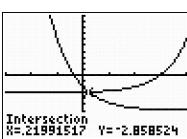
\downarrow translatie $(0, -6)$

$$g(x) = 4 \cdot \left(\frac{1}{3}\right)^x - 6 \text{ met } B_g = \langle -6, \rightarrow \rangle \text{ en H.A.: } y = -6.$$



D10c \square $f(x) = g(x)$ (intersect) $\Rightarrow x \approx 0,22$.

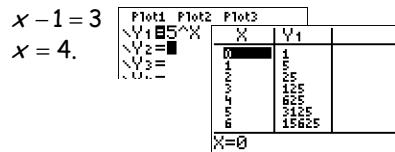
Lees in de grafiek af: $f(x) \geq g(x) \Rightarrow x \geq 0,22$.



D10d \square $B_f = \langle -3, \rightarrow \rangle \Rightarrow f(x) = p$ heeft geen oplossingen voor $p \leq -3$.

D11a \square $5^{x-1} = 125 = 5^3$

$$x-1=3$$

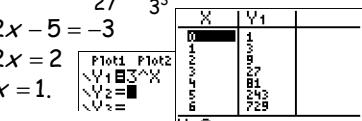


D11b \square $3^{2x-5} = \frac{1}{27} = \frac{1}{3^3} = 3^{-3}$

$$2x-5=-3$$

$$2x=2$$

$$x=1.$$



D11c \square $2 \cdot 4^{2x-1} - 3 = 61$

$$2 \cdot 4^{2x-1} = 64$$

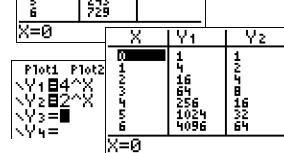
$$4^{2x-1} = 32 = 2^5$$

$$(2^2)^{2x-1} = 2^5$$

$$2^{4x-2} = 2^5$$

$$4x-2=5$$

$$4x=7 \Rightarrow x=\frac{7}{4}=1\frac{3}{4}.$$



D12a \square $7^{x-3} = 20$ (${}^7\log$... nemen)

$$x-3 = {}^7\log(20)$$

$x = 3 + {}^7\log(20)$. heffen elkaar op

D12b \square $6 \cdot 2^x + 5 = 23$

$$6 \cdot 2^x = 18$$

$$2^x = 3$$
 (${}^2\log$... nemen)

$$x = {}^2\log(3).$$

D12c \square $10 \cdot (\frac{1}{2})^{2x-1} = 600$

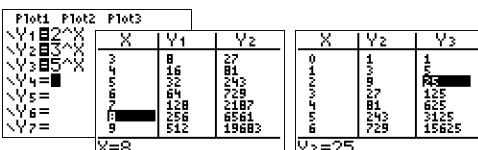
$$(\frac{1}{2})^{2x-1} = 60$$
 ($\frac{1}{2}\log$... nemen)

$$2x-1 = \frac{1}{2}\log(60)$$

$$2x = 1 + \frac{1}{2}\log(60)$$

$$x = \frac{1}{2} + \frac{1}{2} \cdot \frac{1}{2}\log(60).$$

D13a \square ${}^2\log(256) = {}^2\log(2^8) = 8$.



D13b \square ${}^3\log(3 \cdot \sqrt{3}) = {}^3\log(3^1 \cdot 3^{\frac{1}{2}}) = {}^3\log(3^{\frac{3}{2}}) = 1\frac{1}{2}$.

${}^3\log$... en ${}^g\log$... heffen elkaar op

D13c \square ${}^5\log(\frac{1}{25}) = {}^5\log(\frac{1}{5^2}) = {}^5\log(5^{-2}) = -2$.

D14a \square ${}^2\log(x) = -3$ (2^{..} nemen)

$$x = 2^{-3} = \frac{1}{2^3} = \frac{1}{8}.$$

${}^g\log$... en ${}^g\log$... heffen elkaar op

D14b \square ${}^3\log(x-4) = 2$ (3^{..} nemen)

$$x-4 = 3^2 = 9$$

$$x=13.$$

D14c \square ${}^4\log(x^2 - 5) = 1$ (4^{..} nemen)

$$x^2 - 5 = 4^1 = 4$$

$$x^2 = 9$$

$$x = 3 \vee x = -3.$$

D15a \square $y = {}^2\log(x)$ met $D = \langle 0, \rightarrow \rangle$ en V.A.: $x = 0$

\downarrow translatie $(-5, 0)$

$$f(x) = {}^2\log(2x+5) \text{ met } D_f = \langle -5, \rightarrow \rangle \text{ en V.A.: } x = -5.$$

$$y = \frac{1}{2}\log(x) \text{ met } D = \langle 0, \rightarrow \rangle \text{ en V.A.: } x = 0$$

\downarrow verm. t.o.v. de y -as met $\frac{1}{2}$

$$y = \frac{1}{2}\log(2x) \text{ met } D = \langle 0, \rightarrow \rangle \text{ en V.A.: } x = 0$$

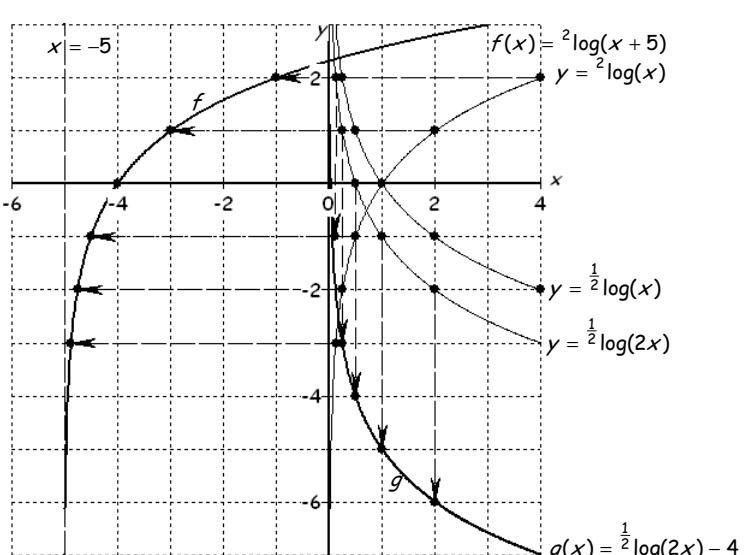
\downarrow translatie $(0, -4)$

$$g(x) = \frac{1}{2}\log(2x) - 4 \text{ met } D_g = \langle 0, \rightarrow \rangle \text{ en V.A.: } x = 0.$$

D15b \square $D_f = \langle -5, \rightarrow \rangle \text{ en } D_g = \langle 0, \rightarrow \rangle$.

Mak de tabel hieronder en de grafiek hiernaast.

x	$\frac{1}{8}$	$\frac{1}{4}$	$\frac{1}{2}$	1	2	4	8
$y = {}^2\log(x)$	-3	-2	-1	0	1	2	3
$y = \frac{1}{2}\log(x)$	3	2	1	0	-1	-2	-3



Gemengde opgaven 7. Exponenten en logaritmen

G24a $\sqrt[4]{a} = a^{\frac{1}{4}}$.

G24c $\frac{\sqrt[3]{a}}{a^2} = \frac{a^{\frac{1}{3}}}{a^2} = a^{\frac{1}{3}-2} = a^{-\frac{5}{3}}$.

G24b $\frac{1}{\sqrt[3]{a}} = \frac{1}{a^{\frac{1}{3}}} = a^{-\frac{1}{3}}$.

G24d $\frac{\sqrt{a}}{a \cdot \sqrt[4]{a}} = \frac{a^{\frac{1}{2}}}{a^1 \cdot a^{\frac{1}{4}}} = \frac{a^{\frac{1}{2}}}{a^{\frac{5}{4}}} = a^{\frac{1}{2}-\frac{5}{4}} = a^{-\frac{3}{4}}$.

G25a $\frac{(3b)^2}{5b} = \frac{9b^2}{5b} = \frac{9b}{5} = 1,8b$.

G25c $\frac{(ab)^{-3}}{ab^{-3}} = \frac{a^{-3}b^{-3}}{ab^{-3}} = a^{-3-1} = a^{-4} = \frac{1}{a^4}$.

G25b $(2b^{-2})^3 + (\frac{1}{2}b^{-3})^2 = 8b^{-6} + \frac{1}{4}b^{-6} = 8\frac{1}{4}b^{-6} = \frac{33}{4} \cdot \frac{1}{b^6} = \frac{33}{4b^6}$.

G25d $(\sqrt{9a})^2 = 9a$.

G26a $T^2 = \frac{4\pi^2 \cdot r^3}{g \cdot R^2} = \frac{4\pi^2}{g \cdot R^2} \cdot r^3 \Rightarrow T = \sqrt{\frac{4\pi^2}{g \cdot R^2} \cdot r^3}$. Dus T is evenredig met $r^{1.5}$.

De evenredigheidsconstante is $\sqrt{\frac{4\pi^2}{g \cdot R^2}} = \sqrt{\frac{4\pi^2}{9.81 \cdot (6.37 \cdot 10^6)^2}} \approx 3.15 \cdot 10^{-7}$. ■

G26b $T^2 = \frac{4\pi^2}{g \cdot R^2} \cdot r^3 \Rightarrow r^3 = \frac{g \cdot R^2}{4\pi^2} \cdot T^2 \Rightarrow r = \sqrt[3]{\frac{g \cdot R^2}{4\pi^2} \cdot T^2}$. Dus r is evenredig met $T^{\frac{2}{3}}$.

De evenredigheidsconstante is $\sqrt[3]{\frac{g \cdot R^2}{4\pi^2}} = \sqrt[3]{\frac{9.81 \cdot (6.37 \cdot 10^6)^2}{4\pi^2}} \approx 2.16 \cdot 10^4$. ■

G26c $T \approx 3.15 \cdot 10^{-7} \cdot r^{1.5}$ met $r = 6.37 \cdot 10^6 + 1.6 \cdot 10^6 = 7.97 \cdot 10^6$.

Dus $T \approx 3.15 \cdot 10^{-7} \cdot (7.97 \cdot 10^6)^{1.5} \approx 7088$ (seconden). Dit zijn (ongeveer) 118 minuten. ■

G26d $r \approx 2.16 \cdot 10^4 \cdot T^{\frac{2}{3}}$ met $T = 24 \cdot 60 \cdot 60$ (seconden).

Dus $r \approx 2.16 \cdot 10^4 \cdot (24 \cdot 60 \cdot 60)^{\frac{2}{3}} \approx 42.21 \cdot 10^6$ (m). ■

De hoogte van een geostationaire baan is $42.21 \cdot 10^6 - 6.37 \cdot 10^6 = 35.84 \cdot 10^6$ m. Dit zijn 35840 km. ■

$$\begin{aligned} & 42.21 - 6.37 \\ & *10^6 \quad 35.84 \\ & \text{Ans}/10^6 \quad 35840 \end{aligned}$$

G27a $y = 2^x$ met $B = \langle 0, \rightarrow \rangle$ en H.A.: $y = 0$

↓verm. t.o.v. de x -as met $\frac{1}{10}$

$y = \frac{1}{10} \cdot 2^x$ met $B = \langle 0, \rightarrow \rangle$ en H.A.: $y = 0$

↓translatie $(-3, -8)$

$f(x) = \frac{1}{10} \cdot 2^{x+3} - 8$ met $B_f = \langle -8, \rightarrow \rangle$ en H.A.: $y = -8$.

$y = \left(\frac{1}{2}\right)^x$ met $B = \langle 0, \rightarrow \rangle$ en H.A.: $y = 0$

↓translatie $(2, -4)$

$g(x) = \left(\frac{1}{2}\right)^{x-2} - 4$ met $B_g = \langle -4, \rightarrow \rangle$ en H.A.: $y = -4$.

G27b $B_f = \langle -8, \rightarrow \rangle$ en $B_g = \langle -4, \rightarrow \rangle$.

Zie de grafiek hiernaast. (zie tabel op de GR hierboven)

G27c $f(2) = -4.8$. Nu aflezen in grafiek/plot: $x \leq 2 \Rightarrow -8 < x \leq -4.8$.

G27d Er geldt $g(p) - f(p) = 6 \vee f(p) - g(p) = 6$.

$g(p) - f(p) = 6$ (intersect) $\Rightarrow p \approx 0.39$.

$f(p) - g(p) = 6 \Rightarrow g(p) - f(p) = -6$ (intersect) $\Rightarrow p \approx 3.69$.

Dus $p \approx 0.39 \vee p \approx 3.69$.

G27e $f(x) = a$ heeft één oplossing en $g(x) = a$ heeft geen oplossing.

Aflezen in de grafieken: $-8 < a \leq -4$.

G28a $2^{\frac{1}{2}x-2} = 32 = 2^5$

$\frac{1}{2}x - 2 = 5$

$\frac{1}{2}x = 7 \Rightarrow x = 14$.

G28c $5^{2x+1} = 2$ ($^5\log$... nemen)

$2x+1 = ^5\log(2)$

$2x = ^5\log(2) - 1$

$x = \frac{1}{2} \cdot ^5\log(2) - \frac{1}{2}$.

G28e $3 \cdot 2^{5x-2} + 12 = 27$

$3 \cdot 2^{5x-2} = 15$

$2^{5x-2} = 5$ ($^2\log$... nemen)

$5x-2 = ^2\log(5)$

$5x = ^2\log(5) + 2 \Rightarrow x = \frac{1}{5} \cdot ^2\log(5) + \frac{2}{5}$

G28b $3^{5-2x} = 81 = 3^4$

$5-2x = 4$

$-2x = -1 \Rightarrow x = \frac{1}{2}$.

G28d $6^{2x} + 4 = 220$

$6^{2x} = 216 = 6^3$

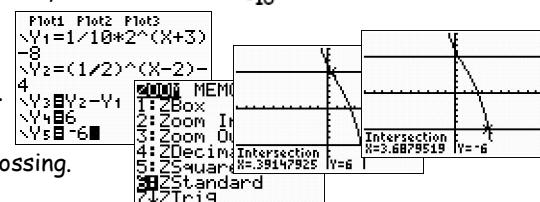
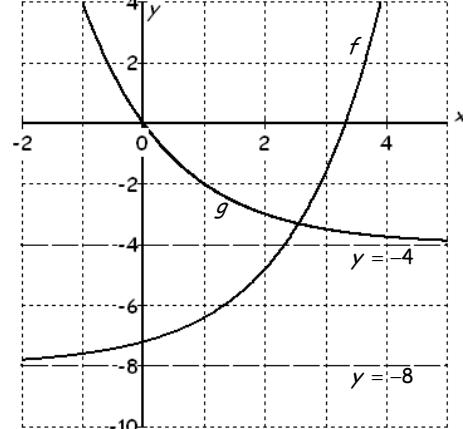
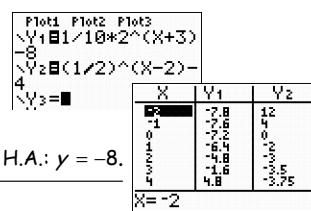
$2x = 3 \Rightarrow x = 1\frac{1}{2}$.

G28f $128 - 4 \cdot 3^{x+1} = 20$

$-4 \cdot 3^{x+1} = -108$

$3^{x+1} = 27 = 3^3$

$x+1 = 3 \Rightarrow x = 2$.



G29a \square $2\log(x^2 - 5) = 3$ (2nd nemen)
 $x^2 - 5 = 2^3 = 8$
 $x^2 = 13$
 $x = -\sqrt{13} \vee x = \sqrt{13}.$

G29c \square $\log(10x + 100) = 3$ (10th nemen)
 $10x + 100 = 10^3 = 1000$
 $10x = 900$
 $x = 90.$

G29e \square $x\log(16) = 2$ (x^{th} nemen)
 $16 = x^2$
 $x = -4$ (vold. niet) $\vee x = 4.$

G29b \square $10^{0,02x} = 5$ (10th log(... nemen))
 $0,02x = \log(5)$ $\boxed{0.02 \rightarrow \text{Frac}} \quad \boxed{1/50}$
 $x = 50 \cdot \log(5).$ ■

G29d \square $5 - 3\log(x^2 + 6) = 3$
 $-3\log(x^2 + 6) = -2$
 $3\log(x^2 + 6) = 2$ (3rd nemen)
 $x^2 + 6 = 3^2 = 9$
 $x^2 = 3 \Rightarrow x = -\sqrt{3} \vee x = \sqrt{3}.$

G29f \square $9\log(3) = x$ (9th nemen)
 $3 = 9^x = (3^2)^x = 3^{2x}$
 $1 = 2x \Rightarrow x = \frac{1}{2}.$

G30a \square $y = 2\log(x)$ met $D = \langle 0, \rightarrow \rangle$ en V.A.: $x = 0$
 \downarrow translatie (1, 0)
 $f(x) = 2\log(x-1)$ met $D_f = \langle 1, \rightarrow \rangle$ en V.A.: $x = 1.$

$y = 2\log(x)$ met $D = \langle 0, \rightarrow \rangle$ en V.A.: $x = 0$
 \downarrow verm. t.o.v. de x -as met -1
 $y = -2\log(x)$ met $D = \langle 0, \rightarrow \rangle$ en V.A.: $x = 0$
 \downarrow translatie (-1, 2)
 $g(x) = -2\log(x+1) + 2$ met $D_g = \langle -1, \rightarrow \rangle$ en V.A.: $x = -1.$

G30b \square $2\log(x-1) = \frac{1}{2}$ (2nd nemen)
 $x-1 = 2^{\frac{1}{2}} = \sqrt{2}$
 $x = \sqrt{2} + 1.$

$\boxed{\begin{array}{l} \sqrt{2}+1 \\ 2 \cdot 414213562 \\ 2 \cdot 2^{-1} \\ 1.828427125 \end{array}}$ ■

$-2\log(x+1) + 2 = \frac{1}{2}$
 $-2\log(x+1) = -1\frac{1}{2}$
 $2\log(x+1) = 1\frac{1}{2}$ (2nd nemen)
 $x+1 = 2^{1\frac{1}{2}} = 2^1 \cdot 2^{\frac{1}{2}} = 2 \cdot \sqrt{2}$
 $x = 2 \cdot \sqrt{2} - 1.$

Dus $AB = 1 + \sqrt{2} - (2 \cdot \sqrt{2} - 1) = 1 + \sqrt{2} - 2 \cdot \sqrt{2} + 1 = 2 - \sqrt{2}.$

G31a \square $t_b = 80; t_f = 20$ en $d = 0,04 \Rightarrow \alpha_c = 3,97(80-20)^{0,233} \cdot 0,04^{-0,3} \approx 27,1.$ ■

$\boxed{\begin{array}{l} 3.97*(80-20)^{0.2} \\ 33+0.04^{-0.3} \\ 27.06959454 \end{array}}$ ■

G31b \square $t_b = 70; t_f = 22$ en $\alpha_c = 23,4 \Rightarrow 23,4 = 3,97(70-22)^{0,233} \cdot d^{-0,3}$
 $d^{-0,3} = \frac{23,4}{3,97(70-22)^{0,233} \cdot d^{-0,3}} = 2,39 \dots \Rightarrow d = \sqrt[3]{\text{Ans}} \approx 0,055$ (m). ■

$\boxed{\begin{array}{l} 23.4/(3.97*(70-22) \\ 3^{\wedge}0.233) \\ 2.391641839 \\ (-0.3)^{\wedge}3 \text{ Ans} \\ .0546612458 \end{array}}$ ■

G31c \square $d = 0,08; t_f = 20$ en $\alpha_c = 21,5 \Rightarrow 21,5 = 3,97(t_b - 20)^{0,233} \cdot 0,08^{-0,3}$
 $(t_b - 20)^{0,233} = \frac{21,5}{3,97 \cdot 0,08^{-0,3}} = 2,5 \dots \Rightarrow t_b = \sqrt[3]{\text{Ans}} + 20 \approx 74$ (°C). ■

$\boxed{\begin{array}{l} 21.5/(3.97*0.08^ \\ 0.3) \\ 0.233^{\wedge}3 \text{ Ans} \\ 54.49707244 \\ \text{Ans}+20 \\ 74.49707244 \end{array}}$ ■

G32a \square $S_{\text{André}} = 12,62 - 0,2 \cdot (52,2 - 50) = 12,18$ en $S_{\text{Bernard}} = 16,37 - 0,2 \cdot (74,1 - 50) = 11,55.$ ■

Nu is de score van André de hoogste score.

G32b \square $12,62 - k \cdot (52,2 - 50) = 16,37 - k \cdot (74,1 - 50)$
 $12,62 - 2,2 \cdot k = 16,37 - 24,1 \cdot k$
 $21,9 \cdot k = 3,75 \Rightarrow k \approx 0,171.$

$\boxed{\begin{array}{l} 24.1-2.2 \\ 16.37-12.62 \\ 21.9 \\ \text{Ans}/21.9 \\ .1712328767 \end{array}}$ ■

G32c \square $S_{\text{Cor}} = 14,32 - 0,1 \cdot (G - 50) = 14,21 \Rightarrow -0,1 \cdot (G - 50) = -0,11 \Rightarrow G - 50 = 1,1 \Rightarrow G = 51,1.$
 $T_{\text{Cor}} = 14,32 \cdot \left(\frac{50}{51,1}\right)^{\frac{2}{3}} \approx 14,11.$ ■

$\boxed{\begin{array}{l} 14.21-14.32 \\ \text{Ans}/-0.1 \\ 1.1 \\ \text{Ans}+50 \\ 51.1 \end{array}}$ ■

G32d \square $S = 15,71 - k \cdot (101 - 50) = 15,71 - 51k$ en $T = 15,71 \cdot \left(\frac{50}{101}\right)^{\frac{2}{3}}.$

$S = T \Rightarrow 15,71 - 51k = 15,71 \cdot \left(\frac{50}{101}\right)^{\frac{2}{3}}$ (intersect of)
 $-51k = 15,71 \cdot \left(\frac{50}{101}\right)^{\frac{2}{3}} - 15,71 \Rightarrow k \approx 0,115.$

$S < T$ (zie een plot) $\Rightarrow k > 0,115.$

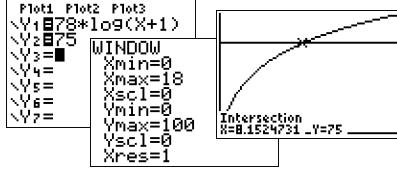


G33a \square Voor $x = 18$ is $P = 100 \Rightarrow 100 = a \cdot \log(19) \Rightarrow a = \frac{100}{\log(19)} \approx 78,201.$ ■

$\boxed{100/\log(19)}$ ■

G33b \square $78 \cdot \log(x+1) = 75$ (intersect of)

$\log(x+1) = \frac{75}{78}$
 $x+1 = 10^{\frac{75}{78}}$
 $x = 10^{\frac{75}{78}} - 1 \approx 8,15.$ Dus op stand 8,2.



G33c \square $K = -1,3$ (bij een knop van 0 tot 6 zou de knop 1,7 aanwijzen) $\Rightarrow x = \frac{1,7}{6} \cdot 18 = 5,1.$

$P = 78 \cdot \log(5,1+1) \approx 61,3.$

Dus P is ongeveer 61% ■

$\boxed{\begin{array}{l} 1.7/6*18 \\ 78*\log(5.1+1) \\ 5.1 \end{array}}$ ■